Caltech

Learning for Safety-Critical Control in Dynamical Systems

Yisong Yue

Policy/Controller Learning (Reinforcement & Imitation)



Non-learning approaches include: optimal control, robust control, adaptive control, etc.

Imitation Learning Tutorial

https://sites.google.com/view/icml2018-imitation-learning/

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Many Exciting Success Stories









" I want to use deep learning to optimize the design, manufacturing and operation of our aircrafts. But I need some guarantees." -- Aerospace Director





Behavioral Guarantees

Possibly Others:

- Fairness lacksquare
- Low-risk ullet

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Temporal logic

Research Questions



- How to constrain learning to (provably) satisfy guarantees?
- How to integrate domain knowledge from physics & control theory?
 - (Towards) a unified framework?
- How to exploit structure for faster learning?
 - (both computational & statistical)

Integration of Learning at Varying Levels

Integration in control/action

Integration in dynamics modeling

• Integration in optimization problem









Functional Regularization (to a certified controller) $argmin_{h}L(h)$ $argmin_{h,g}L(h) + \lambda \|h - g\|^2$ s.t. $\exists g \in G : \|h - g\|^2 < \kappa$ **Model-Based Controllers** (certified by construction) Key idea: G encodes domain knowledge & guarantees $V(x_1, x_2)$ Ideal Behavior Safetv Smoothness

Blended Policy Class (solution concept)





Smooth Imitation Learning for Online Sequence Prediction, Hoang Le, Andrew Kang, Yisong Yue, Peter Carr. ICML 2016 Control Regularization for Reduced Variance Reinforcement Learning, Richard Cheng, Abhinav Verma, et al. ICML 2019



Smooth Imitation Learning for Online Sequence Prediction Hoang Le, Andrew Kang, Yisong Yue, Peter Carr. ICML 2016

Theoretical Guarantees

$$argmin_{h=(f,g)}L(h) \quad \text{s.t.} \quad h(s) = argmin_{a'}(f(s) - a')^2 + \lambda(g(s) - a')^2$$
$$= \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

- By construction: h "close" to g
 - Certifications on g => (relaxed) certifications on h
- Compatible with IL/RL
 - New learning approaches
- Very data efficient

Run-time regularization

Convergence analysis

Low-Variance Gradients

Comments on Certified by Construction

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

- Assumption: all $g \in G$ are certified by construction
 - Robust against disturbances
 - Satisfied for many physical systems
- **Disturbance:** Black box predictor $f \in F$ is a "disturbance" of g
 - Worst-case disturbance depends $\max f(s)$ and λ
 - Guarantees worsen as λ decreases
- Note: local guarantee at the per-state level

Comments on Optimization/Learning

$$argmin_{h=(f,g)}L(h) \quad \text{s.t.} \quad h(s) = argmin_{a'}(f(s) - a')^2 + \lambda(g(s) - a')^2$$
$$= \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

- Alternating optimization
 - Hold g fixed, optimize f
 Hold h fixed, optimize g

 Reduces to "standard" approaches
 - (see NeurIPS 2019 paper for clean treatment)

Imitation-Projected Programmatic Reinforcement Learning Abhinav Verma, Hoang Le, Yisong Yue, Swarat Chaudhuri. NeurIPS 2019



Naïve Approach

- Supervised learning of demonstration data
 - Train predictor per frame
 - Predict per frame



In practice, 2-step smoothing:





Hoang Le, Andrew Kang, Yisong Yue, Peter Carr. ICML 2016



Smooth Imitation Learning for Online Sequence Prediction Hoang Le, Andrew Kang, Yisong Yue, Peter Carr. ICML 2016

Our Results



Time

Smooth Imitation Learning for Online Sequence Prediction Hoang Le, Andrew Kang, Yisong Yue, Peter Carr. ICML 2016

Qualitative Comparison

2-Step Ba

Learning Online Smooth P Operators to ha





Richard Cheng

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

- f is black box
- g is "control prior" (e.g., H-infinity controller)
- Learn f using any RL method

Control Regularization for Reduced Variance Reinforcement Learning Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Richard Cheng

• (Relaxed) Lyapunov stability bounds:



Control Regularization for Reduced Variance Reinforcement Learning

Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Richard Cheng

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

- Theorem (informal):
 - Variance of policy gradient decreases by factor of: $\left(\frac{1}{1+\lambda}\right)^2$

Implies much faster learning!

• Bias converges to:
$$\left(\frac{\lambda}{1+\lambda}\right) D_{TV}(h^*, g)$$

Control Regularization for Reduced Variance Reinforcement Learning

Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Control Regularization for Reduced Variance Reinforcement Learning

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Richard Cheng



Summary: Functional Regularization

Regularization ↔ Constrained Learning



Hybrid Policy Solution Concept

$$h(s) = argmin_{a'}(f(s) - a')^2 + \lambda(g(s) - a')^2$$
$$= \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

Summary: Functional Regularization (cont.)

- Control methods => analytic guarantees
- Blend w/ learning => improve precision/flexibility
- Preserve side guarantees
- Interpret as functional regularization
- Other directions:

Batch Policy Learning under Constraints Hoang Le, Cameron Voloshin, Yisong Yue. ICML 2019

Imitation-Projected Programmatic Reinforcement Learning Abhinav Verma, Hoang Le, Yisong Yue, Swarat Chaudhuri. NeurIPS 2019 (side guarantees)

(real-world improvements)

(possibly relaxed)

(speeds up learning)

(offline learning)

(programmatic controllers)

Integration of Learning at Varying Levels

Integration in control/action



• Integration in optimization problem







Model-Based Control



(Value Iteration is also contraction mapping)

Robust/Optimal Control (fancy contraction mappings)

- Stability guarantees (e.g., Lyapunov)
- Precision/optimality depends on error

Learning Residual Dynamics

F = nominal dynamics \tilde{F} = learned dynamics



Leverage robust/optimal control (fancy contraction mappings)

- Preserve stability (even using deep learning)
- Requires \tilde{F} Lipschitz & bounded error



Shi

O'Connell

Shi

Stable Drone Landing





Neural Lander: Stable Drone Landing Control using Learned Dynamics

Guanya Shi, Xichen Shi, Michael O'Connell, Rose Yu, Kamyar Azizzadenesheli, Anima Anandkumar, Yisong Yue, Soon-Jo Chung. ICRA 2019

Learn the Residual• Dynamics:
$$\begin{pmatrix} \dot{\mathbf{p}} = \mathbf{v}, & m\dot{\mathbf{v}} = m\mathbf{g} + R\mathbf{f}_u + \mathbf{f}_a \\ \dot{R} = RS(\omega), & J\dot{\omega} = J\omega \times \omega + \tau_u + \tau_a \end{pmatrix}$$
• Control:
$$\begin{pmatrix} \mathbf{f}_u = [0, 0, T]^\top \\ \boldsymbol{\tau}_u = [\tau_x, \tau_y, \tau_z]^\top \\ \begin{bmatrix} T \\ \tau_x \\ \tau_z \end{bmatrix} = \begin{bmatrix} c_T & c_T & c_T & c_T \\ 0 & c_T l_{arm} & 0 \\ -c_T l_{arm} & 0 & c_T l_{arm} \\ 0 & c_T l_{arm} & 0 \\ -c_T l_{arm} & 0 & c_T l_{arm} \\ c_Q & -c_Q & c_Q \end{bmatrix} \begin{bmatrix} n_1^2 \\ n_2^2 \\ n_3^2 \\ n_4^2 \end{bmatrix}$$
• Unknown forces & moments:
$$\begin{pmatrix} \mathbf{f}_a = [f_{a,x}, f_{a,y}, f_{a,z}]^\top \\ \boldsymbol{\tau}_a = [\tau_{a,x}, \tau_{a,y}, \tau_{a,z}]^\top \end{pmatrix}$$
Learn the Residual

Data Collection (Manual Exploration)

Notable Extension: Safe Exploration





Spectral-Normalized

4-Layer Feed-Forward

• Learn ground effect: $\tilde{F}(s, u) \rightarrow \mathbf{f}_a = [f_{a,x}, f_{a,y}, f_{a,z}]^\top$

• (s,u): height, velocity, attitude and four control inputs

Prediction Results



Neural Lander: Stable Drone Landing Control using Learned Dynamics

Guanya Shi, Xichen Shi, Michael O'Connell, Rose Yu, Kamyar Azizzadenesheli, Anima Anandkumar, Yisong Yue, Soon-Jo Chung. ICRA 2019.

Prediction Results



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a Xichen Michael Shi O'Connell

Controller Design (simplified)

• Nonlinear Feedback Linearization:

$$u_{nominal} = K_s \eta$$
 $\eta = \begin{bmatrix} p - p^* \\ v - v^* \end{bmatrix}$ Desired Trajectory (tracking error)
Feedback Linearization (PD control)

• Cancel out ground effect $\tilde{F}(s, u_{old})$: $u = u_{nominal} + u_{residual}$ Requires Lipschitz & small time delay



uanya Xichen Michael Shi Shi O'Connell

Controller Design (simplified)

• Nonlinear Feedback Linearization:

$$u_{nominal} = K_s \eta$$
 $\eta = \begin{bmatrix} p - p^* \\ v - v^* \end{bmatrix}$ Desired Trajectory (tracking error)







Aside: Robust Regression for Safe Exploration

• Robust regression for provable extrapolation => Safe Exploration!





Provably safe trajectory planning for exploration!

Robust Regression for Safe Exploration in Control,

Angie Liu, Guanya Shi, Soon-Jo Chung, Anima Anandkumar, Yisong Yue, L4DC 2020

Chance-Constrained Trajectory Optimization for Safe Exploration and Learning of Nonlinear Systems,

Yashwanth Kumar Nakka, Angie Liu, Guanya Shi, Anima Anandkumar, Yisong Yue, Soon-Jo Chung, R-AL 2021





Yashwanth

Nakka

Angie Liu

Aside: Learning Control Lyapunov/Barrier Functions

- CLFs & CBFs encode low-dimensional projection of dynamics
 - DOF of action space rather than state space
 - Can be easier to learn than full dynamics
- How to learn CLF/CBF for controller design?
- How to analyze stability/safety under uncertainty?

Episodic Learning with Control Lyapunov Functions for Uncertain Robotic Systems
Andrew J. Taylor, Victor D. Dorobantu, Hoang M. Le, Yisong Yue, Aaron D. Ames. IROS 2019.
A Control Lyapunov Perspective on Episodic Learning via Projection to State Stability
Andrew J. Taylor, Victor D. Dorobantu, Meera Krishnamoorthy, Hoang M. Le, Yisong Yue, Aaron D. Ames. CDC 2019.
Learning for Safety-Critical Control with Control Barrier Functions
Andrew Taylor, Andrew Singletary, Yisong Yue, Aaron Ames. L4DC 2020.
A Control Barrier Perspective on Episodic Learning via Projection-to-State Safety
Andrew J. Taylor, Andrew Singletary, Yisong Yue, Aaron D. Ames. L-CSS 2020.





Andrew Taylor

Victor Dorobantu

Summary: Dynamics Learning

- Learn residual dynamics
- Control Lipschitz constant
- Standard controller design

• Robust regression for safe exploration

(data efficient)

(imposes compatible structure)

(inherits guarantees)

(provable limited extrapolation)

Integration of Learning at Varying Levels

Integration in control/action

Integration in dynamics modeling







Model-Based Planning

• Environment model is given

1

 $s_{t+1} = F(s_t, u_t) + \epsilon$

• Design global plan (aka trajectory)







Optimization as Sequential Decision Making

- Many Solvers are Sequential
 - Tree-Search
 - Greedy
 - Gradient Descent
- Can view solver as "agent" or "policy"
 - State = intermediate solution
 - Find a state with high reward (solution)
 - Learn better local decision making

Optimization as Sequential Decision Making

Learning to Search/Plan

- Learning to Search via Retrospective Imitation [arXiv]
- Co-training for Policy Learning [UAI 2019]
- GLAS: Global-to-Local Safe Autonomy Synthesis [RA-L 2020]
- A General Large Neighborhood Search Framework for Solving Integer Programs [NeurIPS 2020]

Submodular Maximization

- Learning Policies for Contextual Submodular Prediction [ICML 2013]
- Learning to Make Decisions via Submodular Regularization [ICLR 2021]

Learning to Infer

- Iterative Amortized Inference [ICML 2018]
- A General Method for Amortizing Variational Filtering [NeurIPS 2018]
- Iterative Amortized Policy Optimization [arXiv]







Jialin Song Ben Riviere







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Joe Marino

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Joe Marino



Ravi Lanka







Jialin Song

Learning to Search via Retrospective Imitation, Jialin Song, Ravi Lanka, et al., arXiv

Ongoing: ENav Integration



Shreyansh Daftry

Olivier Neil Ono Toupet

Siddarth Abcouwer Venkatraman











Left Camera



SCLK: 1,478,818,216.76650

Right Camera



Preliminary Results



Baseline ENav (Cycle Time(s))

	7%	10 %	12 %	15 %
20 deg.	1.45	3.38	n/a	n/a
15 deg.	1.00	2.49	2.89	3.58
10 deg.	0.99	2.39	3.17	2.06
5 deg.	0.77	2.38	3.79	2.09
0 deg.	0.98	2.57	3.44	5.18

MLNav (Cycle Time(s))

	7%	10 %	12 %	15 %
20 deg.	0.80	0.99	n/a	n/a
15 deg.	0.48	0.99	1.20	1.45
10 deg.	0.47	1.20	1.38	1.41
5 deg.	0.54	0.93	1.25	1.28
0 deg.	0.47	1.11	1.33	1.78

Machine Learning Based Path Planning for Improved Rover Navigation, Neil Abcouwer et al., IEEE AeroConf 2021.

Learned Decentralized Planner (enforcing safety)





Ben Riviere



GLAS: Global-to-Local Safe Autonomy Synthesis for Multi-Robot Motion Planning with End-to-End Learning, Benjamin Rivière, et al., R-AL 2020



5. Deploy: Six robots navigating an obstacle course.

2x

Blending Models/Rules & Black-Box Learning



Collaborators



Song



Le

Kang





Wolfgang Guanya Richard Shi Cheng

Abhinav Verma

Angie Liu **Riviere**

Ben





Stephane Siddarth Ayya Yashwanth Alieva Nakka Ross Venkatraman

Robin Jimmy Cameron Andrew

Voloshin Zhou Chen

Lanka

Marino

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Kamyar Michael Aadyot Cvitkovic Azizzadenesheli O'Connell Bhatnagar Debadeepta





Xichen Alex Shi Piche



Shreyansh Stephen Anima Soon-Jo Joel Gabor Olivier Neil Peter Rose Bistra Stephan Jim Swarat Drew Hiro Aaron Mayo Anandkumar Chung Daftry Burdick Little Toupet Abcouwer Carr Yu Dilkina Chen Orosz Chaudhuri Mandt Bagnell Ono Ames





Dorobantu Hoenig

Albert Zhao Krishnamoorthy Dey

Meera

Tyler del Sesto

Alessandro lalongo

Aiden Aceves

References

Smooth Imitation Learning for Online Sequence Prediction, Hoang Le, et al., ICML 2016 Control Regularization for Reduced Variance Reinforcement Learning, Richard Cheng et al. ICML 2019 Batch Policy Learning under Constraints, Hoang Le, et al. ICML 2019 Learning Smooth Online Predictors for Real-Time Camera Planning using Recurrent Decision Trees, Jianhui Chen, et al., CVPR 2016 Imitation-Projected Programmatic Reinforcement Learning, Abhinav Verma, Hoang Le, et al., NeurIPS 2019 Neural Lander: Stable Drone Landing Control using Learned Dynamics, Guanya Shi, et al., ICRA 2019 Neural-Swarm: Decentralized Close-Proximity Multirotor Control Using Learned Interactions, Guanya Shi et al., ICRA 2020 Neural-Swarm2: Planning and Control of Heterogeneous Multirotor Swarms using Learned Interactions, Guanya Shi et al., arXiv **Robust Regression for Safe Exploration in Control**, Angie Liu, Guanya Shi, et al., L4DC 2020 **Chance-Constrained Trajectory Optimization for Safe Exploration and Learning of Nonlinear Systems,** Yashwanth Kumar Nakka, et al. R-AL 2021 Episodic Learning with Control Lyapunov Functions for Uncertain Robotic Systems, Andrew Taylor, Victor Dorobantu, et al., IROS 2019 A Control Lyapunov Perspective on Episodic Learning via Projection to State Stability, Andrew Taylor, Victor Dorobantu, et al., CDC 2019 Learning for Safety-Critical Control with Control Barrier Functions, Andrew Taylor, et al., L4DC 2020 A Control Barrier Perspective on Episodic Learning via Projection-to-State Safety, Andrew Taylor, et al., L-CSS 2020 Learning to Search via Retrospective Imitation, Jialin Song, Ravi Lanka, et al., arXiv **Co-Training for Policy Learning**, Jialin Song, Ravi Lanka, et al., UAI 2019 A General Large Neighborhood Search Framework for Solving Integer Programs, Jialin Song, Ravi Lanka, et al., NeurIPS 2020 GLAS: Global-to-Local Safe Autonomy Synthesis for Multi-Robot Motion Planning with End-to-End Learning, Benjamin Rivière, et al., R-AL 2020 Learning Policies for Contextual Submodular Optimization, Stephane Ross et al., ICML 2013 Learning to Make Decisions via Submodular Regularization, Ayya Alieva, Aiden Aceves, et al., ICLR 2021 Iterative Amortized Inference, Joe Marino et al., ICML 2018 A General Framework for Amortizing Variational Filtering, Joe Marino et al, NeurIPS 2018 **Iterative Amortized Policy Optimization**, Joe Marino et al., arXiv Machine Learning Based Path Planning for Improved Rover Navigation, Neil Abcouwer et al., IEEE AeroConf 2021