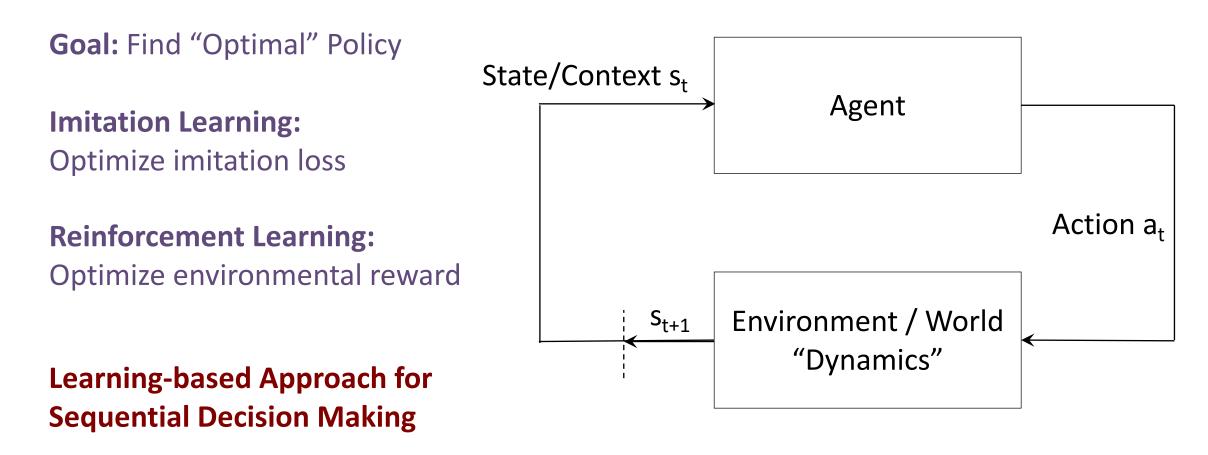
Caltech

Learning for Reliable Control in Dynamical Systems

Yisong Yue

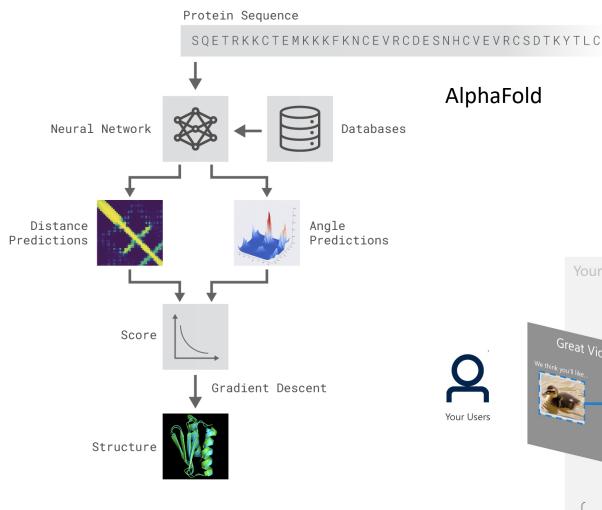
Policy/Controller Learning (Reinforcement & Imitation)



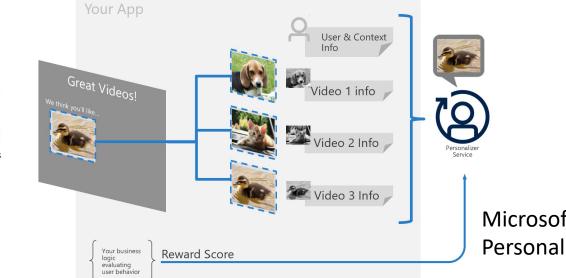
Non-learning approaches include: optimal control, robust control, adaptive control, etc.

Many Exciting Success Stories





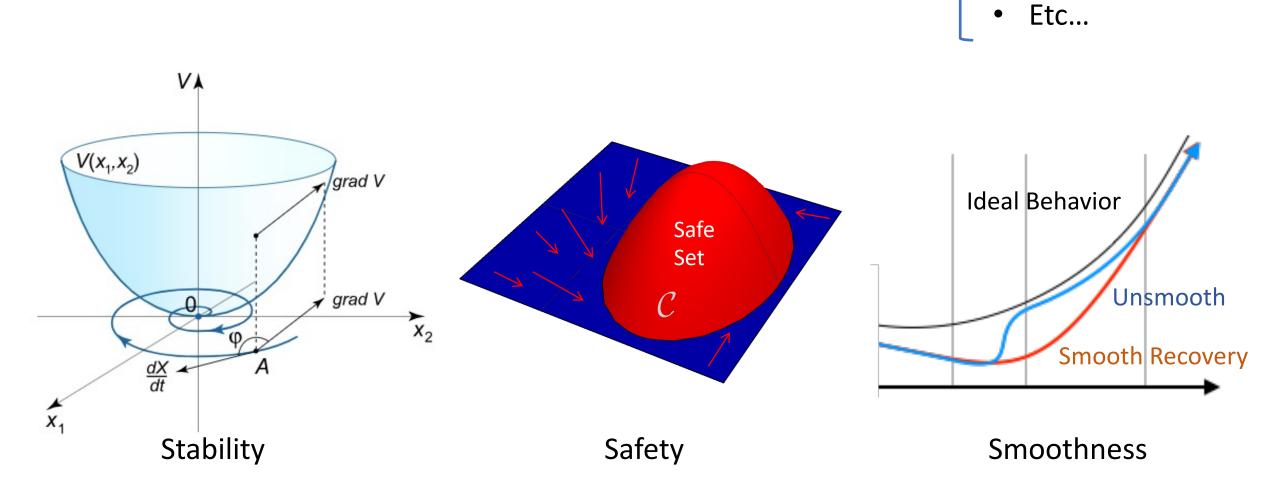




Microsoft Azure Personalizer

" I want to use deep learning to optimize the design, manufacturing and operation of our aircrafts. But I need some guarantees." -- Aerospace Director





Behavioral Guarantees

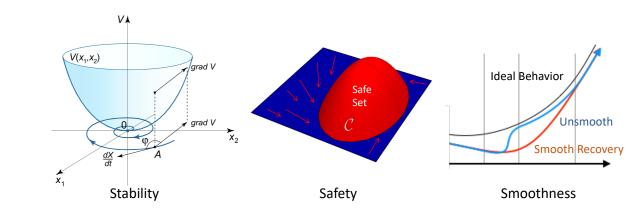
Possibly Others:

- Fairness lacksquare
- Low-risk ullet

•

Temporal logic

Research Questions



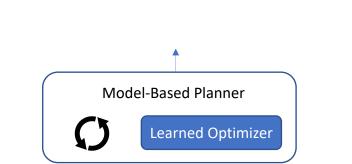
- How to constrain learning to (provably) satisfy guarantees?
- How to integrate domain knowledge from physics & control theory?
 - (Towards) a unified framework?
- How to exploit structure for faster learning?
 - (both computational & statistical)

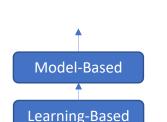
Integration of Learning at Varying Levels

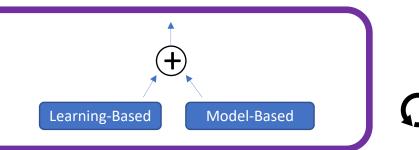
• Integration in control/action

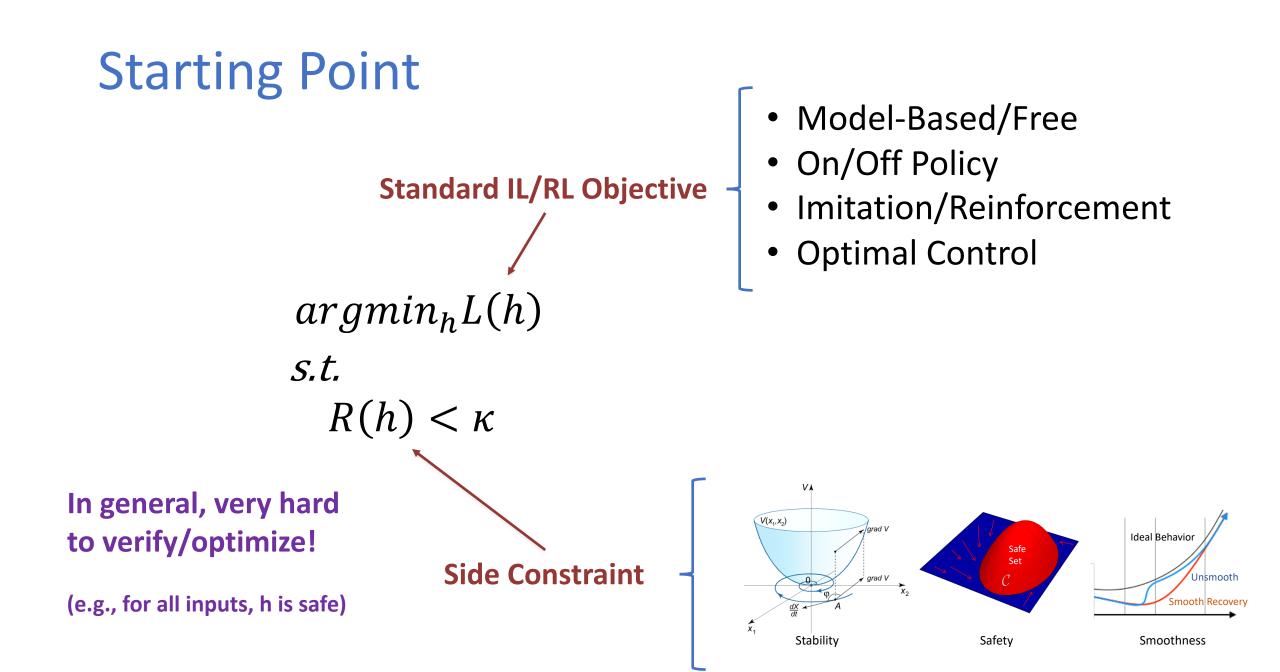
Integration in dynamics modeling

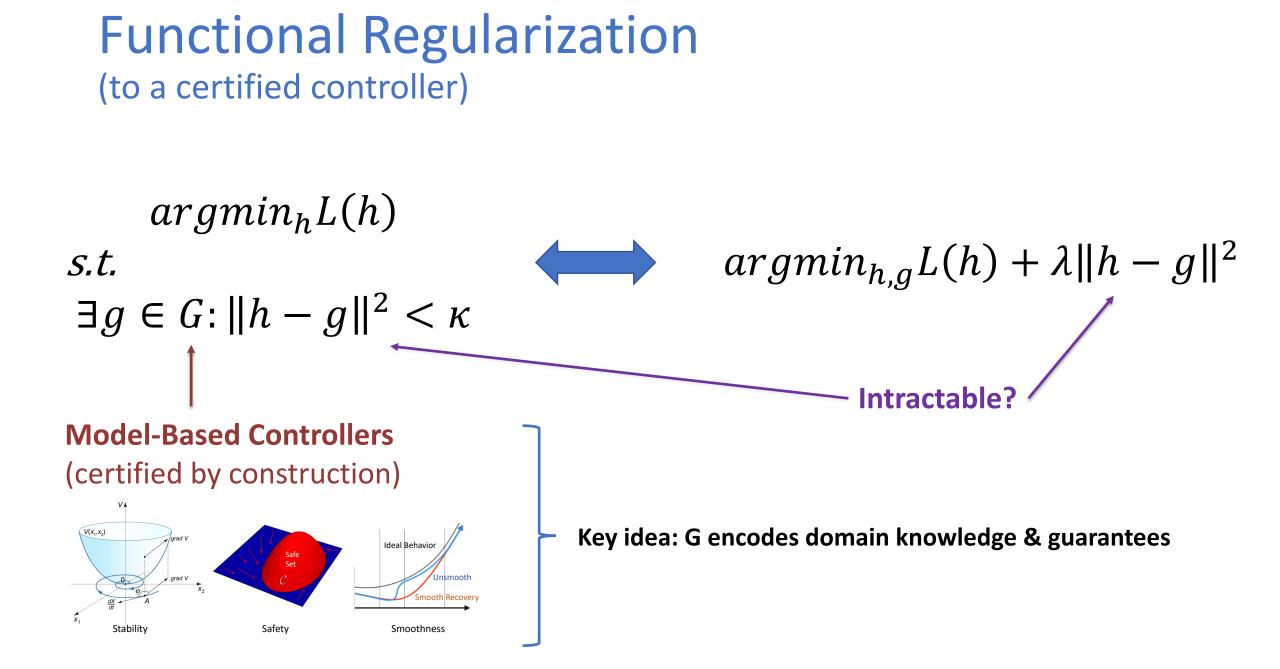
• Integration in optimization problem











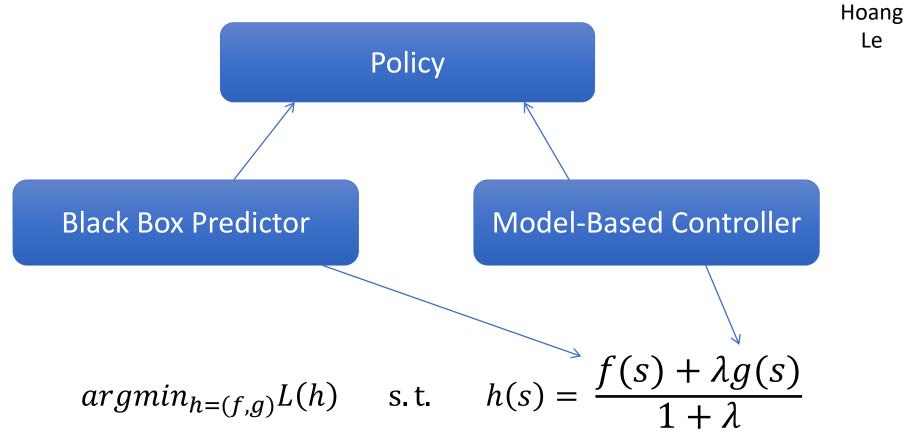
Blended Policy Class (solution concept)



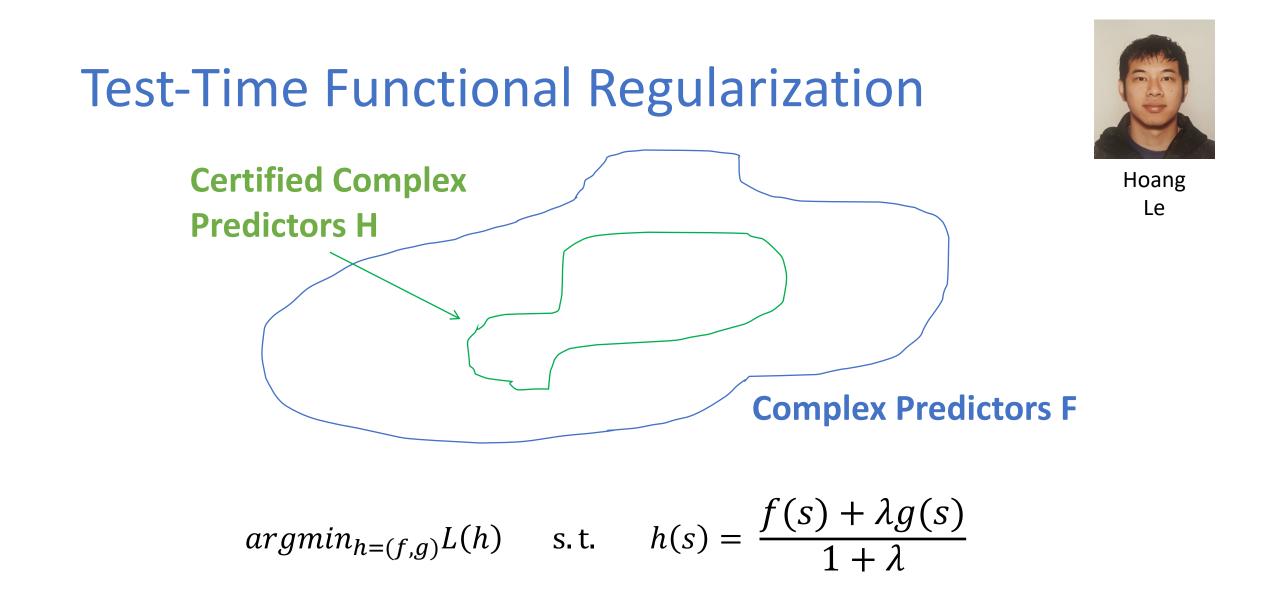
Le

Richard

Cheng



Smooth Imitation Learning for Online Sequence Prediction, Hoang Le, Andrew Kang, Yisong Yue, Peter Carr. ICML 2016 Control Regularization for Reduced Variance Reinforcement Learning, Richard Cheng, Abhinav Verma, et al. ICML 2019



Theoretical Guarantees

$$argmin_{h=(f,g)}L(h)$$
 s.t. $h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$

- By construction: h "close" to g
 - Certifications on g => (relaxed) certifications on h
- Compatible with IL/RL
 - New learning approaches
- Very data efficient

Run-time regularization

Convergence analysis

Low-Variance Gradients

Comments on Certified by Construction

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

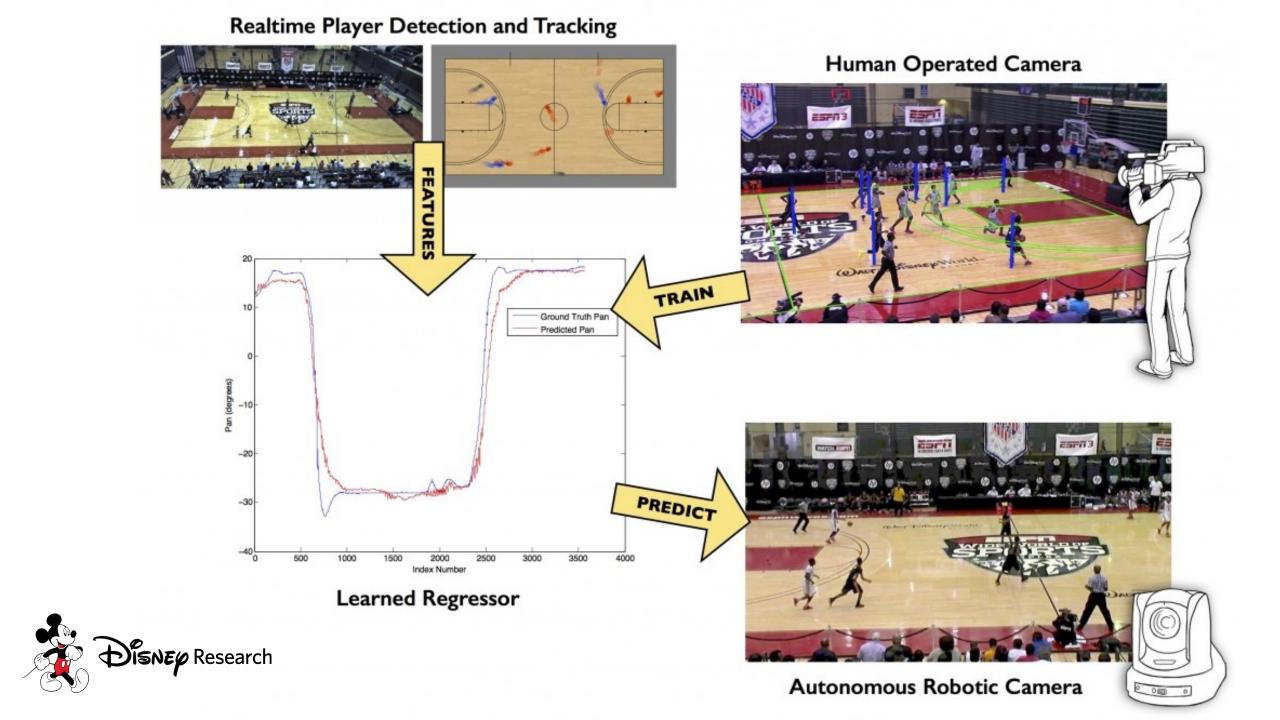
- Assumption: all $g \in G$ are certified by construction
 - Robust against disturbances
 - Satisfied for many physical systems
- **Disturbance:** $f \in F$ is a "disturbance" of g
 - Worst-case disturbance depends $\max f(s)$ and λ
 - Guarantees worsen as λ decreases
- **Note:** local per-state guarantee => global guarantee

Comments on Optimization/Learning

$$argmin_{h=(f,g)}L(h)$$
 s.t. $h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$

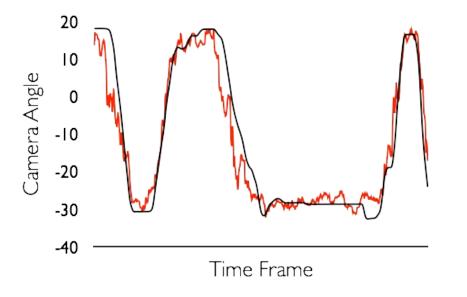
- Alternating optimization
 - Hold g fixed, optimize f
 - Hold h fixed, optimize g
 Reduces to "standard" approaches
 - (see NeurIPS 2019 paper for clean treatment)

Imitation-Projected Programmatic Reinforcement Learning Abhinav Verma, Hoang Le, Yisong Yue, Swarat Chaudhuri. NeurIPS 2019

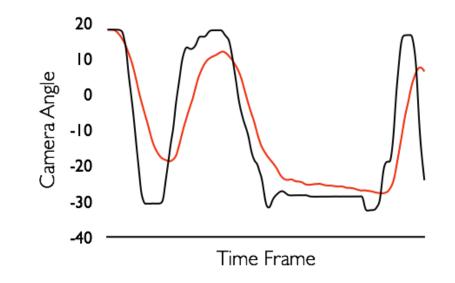


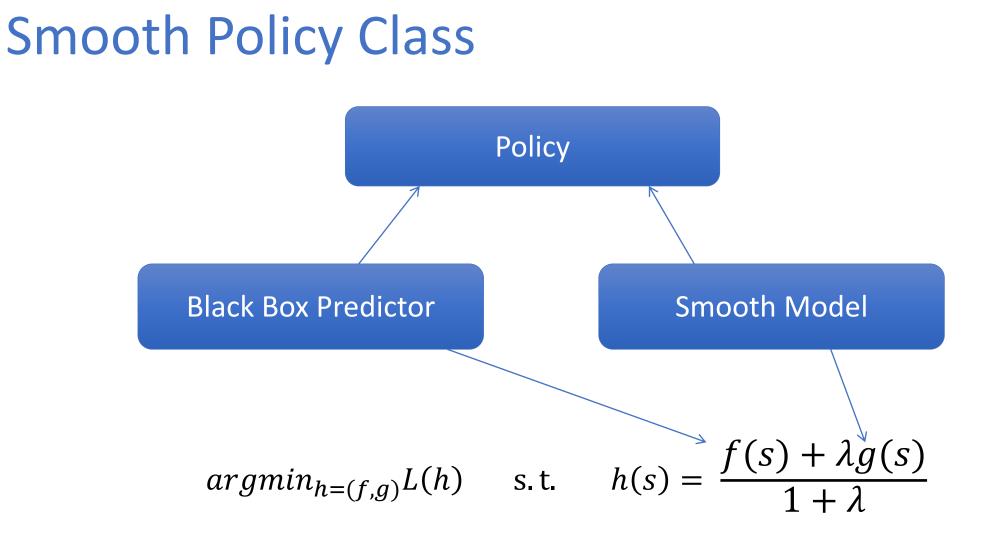
Naïve Approach

- Supervised learning of demonstration data
 - Train predictor per frame
 - Predict per frame



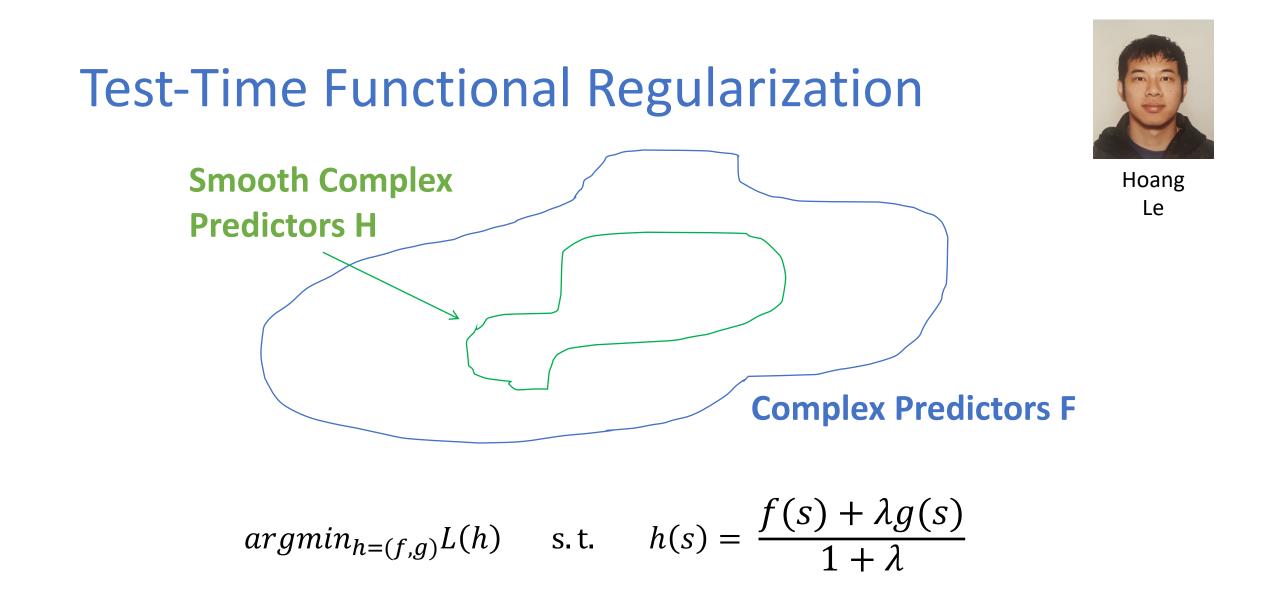
In practice, 2-step smoothing:



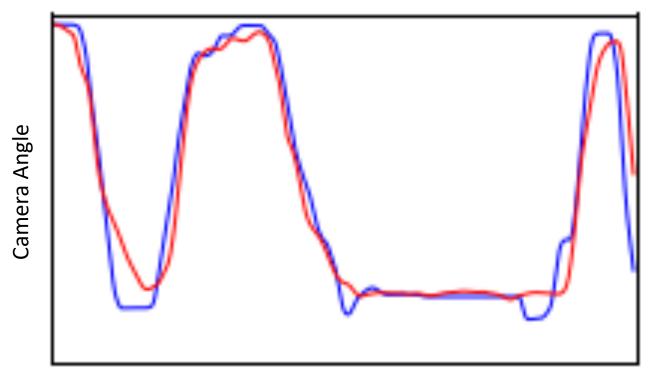


Hoang

Le



Our Results

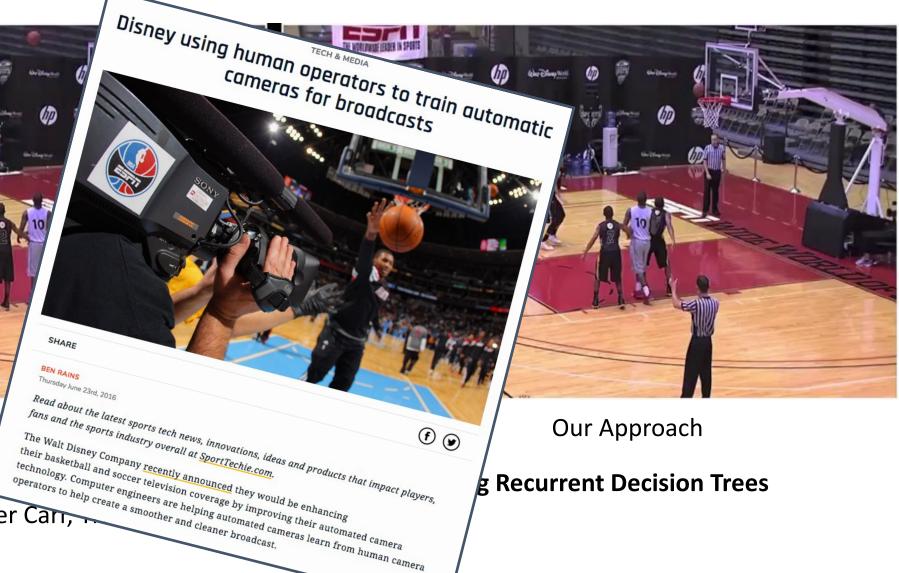


Time

Qualitative Comparison

2-Step Ba

Learning Online Smooth P Jianhui Chen, Hoang Le, Peter Carr,





Richard Cheng

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

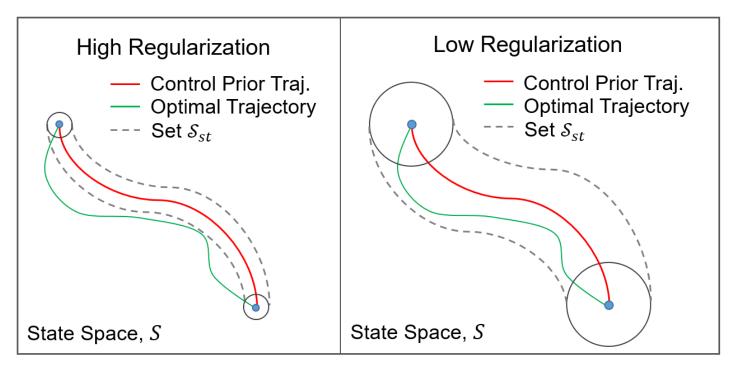
- f is black box
- g is "control prior" (e.g., H-infinity controller)
- Learn f using any RL method

Control Regularization for Reduced Variance Reinforcement Learning Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Richard Cheng

• (Relaxed) Lyapunov stability bounds:



Control Regularization for Reduced Variance Reinforcement Learning

Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Richard Cheng

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

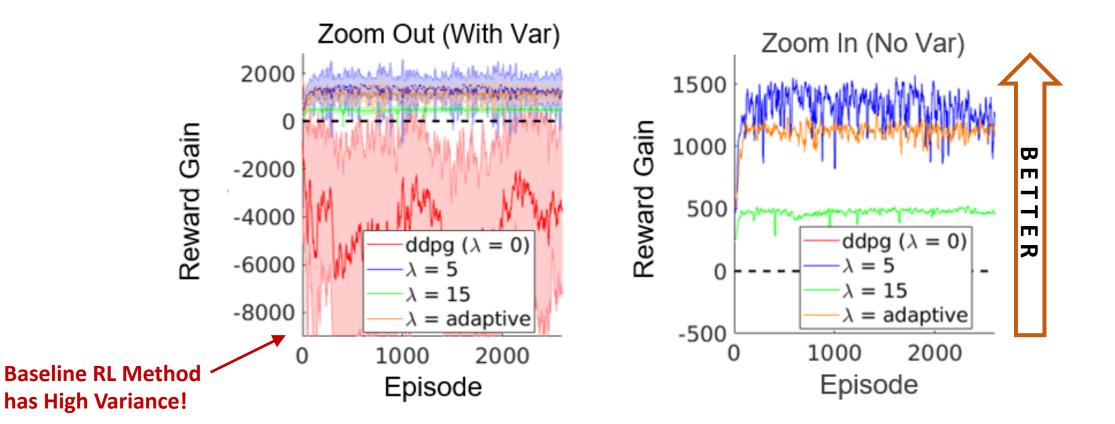
- Theorem (informal):
 - Variance of policy gradient decreases by factor of: $\left(\frac{1}{1+\lambda}\right)^2$

Implies much faster learning!

• Bias converges to:
$$\left(\frac{\lambda}{1+\lambda}\right) D_{TV}(h^*, g)$$

Control Regularization for Reduced Variance Reinforcement Learning

Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Control Regularization for Reduced Variance Reinforcement Learning

Richard Cheng, Abhinav Verma, Gabor Orosz, Swarat Chaudhuri, Yisong Yue, Joel Burdick. ICML 2019



Richard Cheng



Summary: Functional Regularization

Regularization ↔ Constrained Learning



Hybrid Policy Solution Concept

$$h(s) = \frac{f(s) + \lambda g(s)}{1 + \lambda}$$

Summary: Functional Regularization (cont.)

- Control methods => analytic guarantees
- Blend w/ learning => improve precision/flexibility
- Preserve behavioral guarantees
- Interpret as functional regularization
- Other directions:

Batch Policy Learning under Constraints Hoang Le, Cameron Voloshin, Yisong Yue. ICML 2019

Imitation-Projected Programmatic Reinforcement Learning Abhinav Verma, Hoang Le, Yisong Yue, Swarat Chaudhuri. NeurIPS 2019 (side guarantees)

(real-world improvements)

(possibly relaxed)

(speeds up learning)

(offline learning)

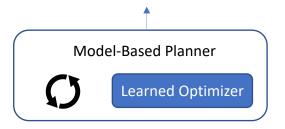
(neurosymbolic policies)

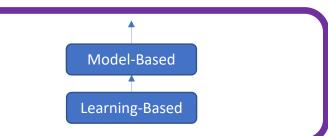
Integration of Learning at Varying Levels

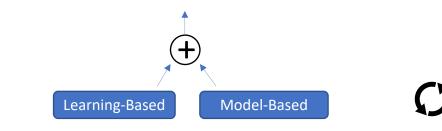
Integration in control/action



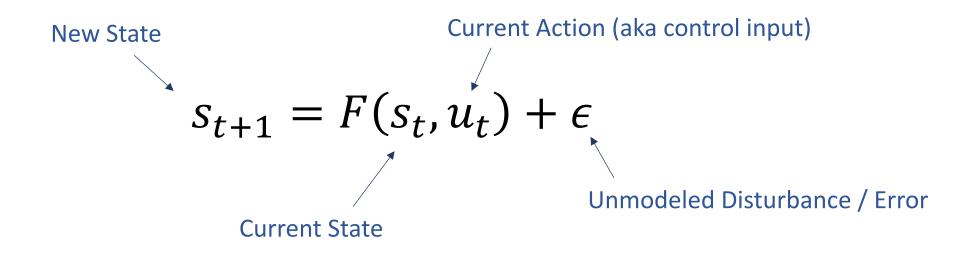
• Integration in optimization problem







Model-Based Control



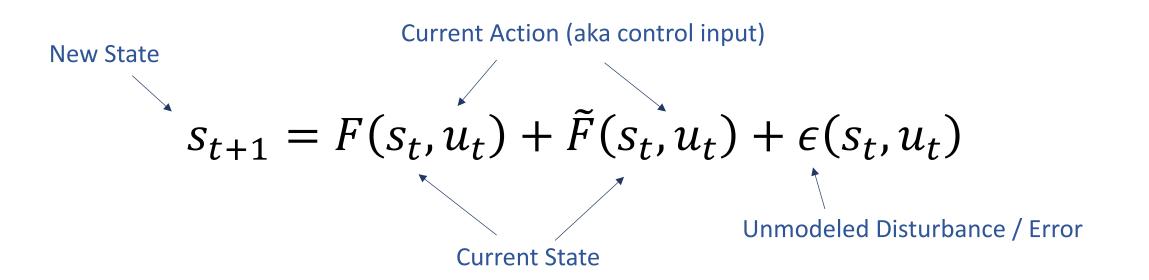
(Value Iteration is also contraction mapping)

Robust/Optimal Control (fancy contraction mappings)

- Stability guarantees (e.g., Lyapunov)
- Precision/optimality depends on error

Learning Residual Dynamics

F = nominal dynamics \tilde{F} = learned dynamics



Leverage robust/optimal control (fancy contraction mappings)

- Preserve stability (even using deep learning)
- Requires \tilde{F} Lipschitz & bounded error

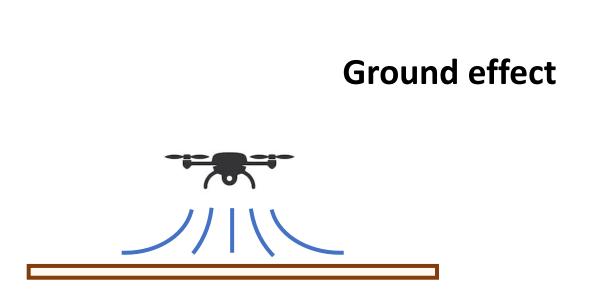


Shi

O'Connell

Shi

Boundary Conditions



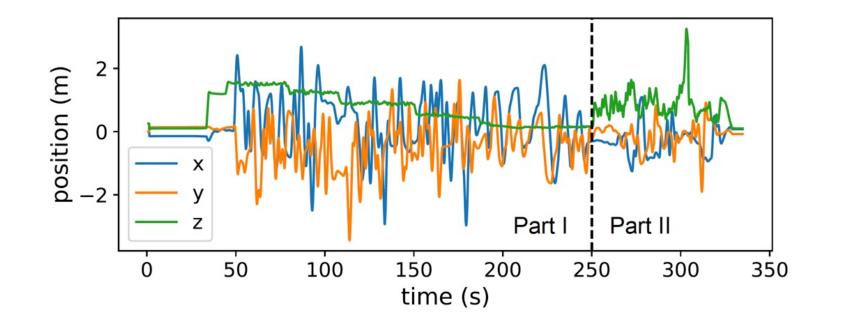


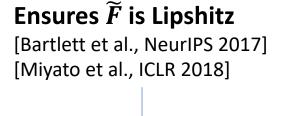
Neural Lander: Stable Drone Landing Control using Learned Dynamics, Guanya Shi, Xichen Shi, Michael O'Connell, et al. ICRA 2019 Neural-Swarm: Decentralized Close-Proximity Multirotor Control Using Learned Interactions, Guanya Shi et al., ICRA 2020 Neural-Swarm2: Planning and Control of Heterogeneous Multirotor Swarms using Learned Interactions, Guanya Shi et al., T-RO 1021

Learn the Residual• Dynamics:
$$\begin{pmatrix} \dot{\mathbf{p}} = \mathbf{v}, & m\dot{\mathbf{v}} = m\mathbf{g} + R\mathbf{f}_u + \mathbf{f}_a \\ \dot{R} = RS(\omega), & J\dot{\omega} = J\omega \times \omega + \tau_u + \tau_a \end{pmatrix}$$
• Control:
$$\begin{cases} \mathbf{f}_u = [0, 0, T]^\top \\ \mathbf{\tau}_u = [\tau_x, \tau_y, \tau_z]^\top \\ \begin{bmatrix} T \\ \tau_x \\ \tau_z \end{bmatrix} = \begin{bmatrix} c_T & c_T & c_T & c_T \\ 0 & c_T l_{arm} & 0 \\ -c_T l_{arm} & 0 & c_T l_{arm} \\ 0 & c_T l_{arm} & 0 \\ c_Q & -c_Q & c_Q \end{bmatrix} \begin{bmatrix} n_1^2 \\ n_2^2 \\ n_3^2 \\ n_4^2 \end{bmatrix}$$
• Unknown forces & moments:
$$\begin{cases} \mathbf{f}_a = [f_{a,x}, f_{a,y}, f_{a,z}]^\top \\ \mathbf{\tau}_a = [\tau_{a,x}, \tau_{a,y}, \tau_{a,z}]^\top \end{cases}$$
Learn the Residual

Data Collection (Manual Exploration)

Notable Extension: Safe Exploration





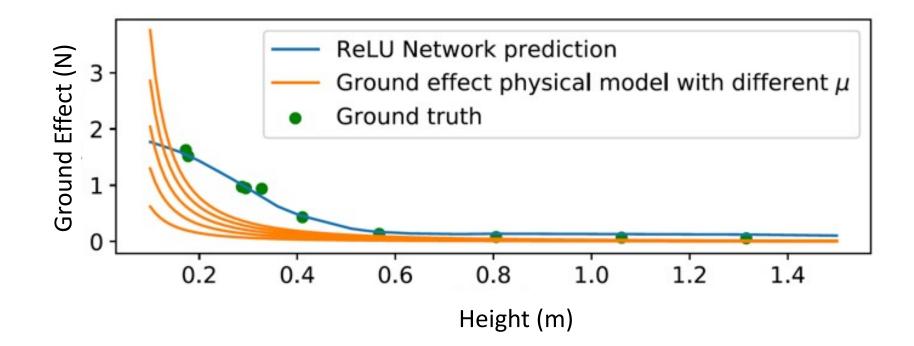
Spectral-Normalized

4-Layer Feed-Forward

• Learn ground effect: $\tilde{F}(s, u) \rightarrow \mathbf{f}_a = [f_{a,x}, f_{a,y}, f_{a,z}]^\top$

• (s,u): height, velocity, attitude and four control inputs

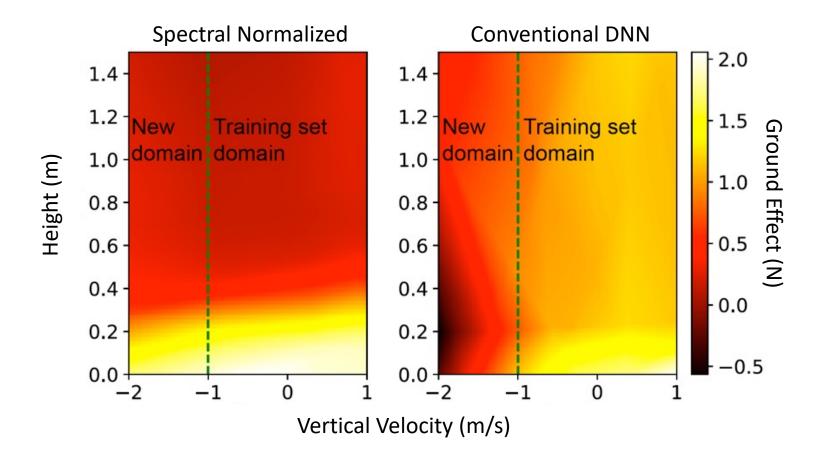
Prediction Results



Neural Lander: Stable Drone Landing Control using Learned Dynamics

Guanya Shi, Xichen Shi, Michael O'Connell, Rose Yu, Kamyar Azizzadenesheli, Anima Anandkumar, Yisong Yue, Soon-Jo Chung. ICRA 2019.

Prediction Results



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Shi

Gichen Michael Shi O'Connell

Controller Design (simplified)

• Nonlinear Feedback Linearization:

$$u_{nominal} = K_s \eta$$
 $\eta = \begin{bmatrix} p - p^* \\ v - v^* \end{bmatrix}$ Desired Trajectory (tracking error)
Feedback Linearization (PD control)

• Cancel out ground effect $\tilde{F}(s, u_{old})$: $u = u_{nominal} + u_{residual}$ / Requires Lipschitz & small time delay



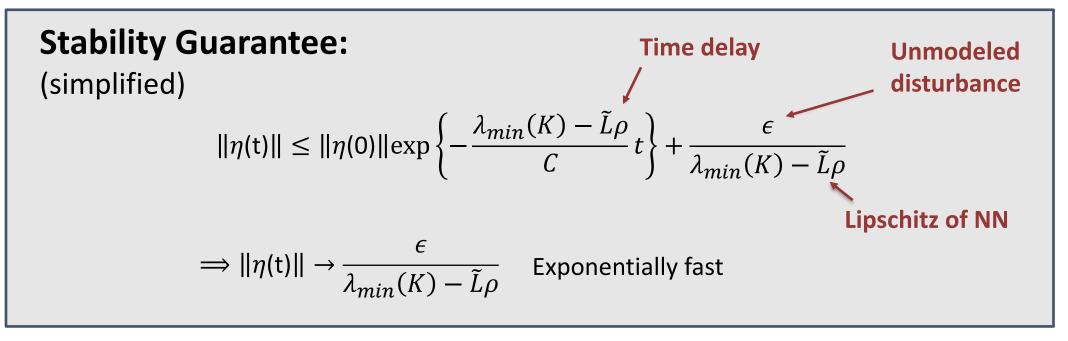
Shi

Xichen Michael Shi O'Connell

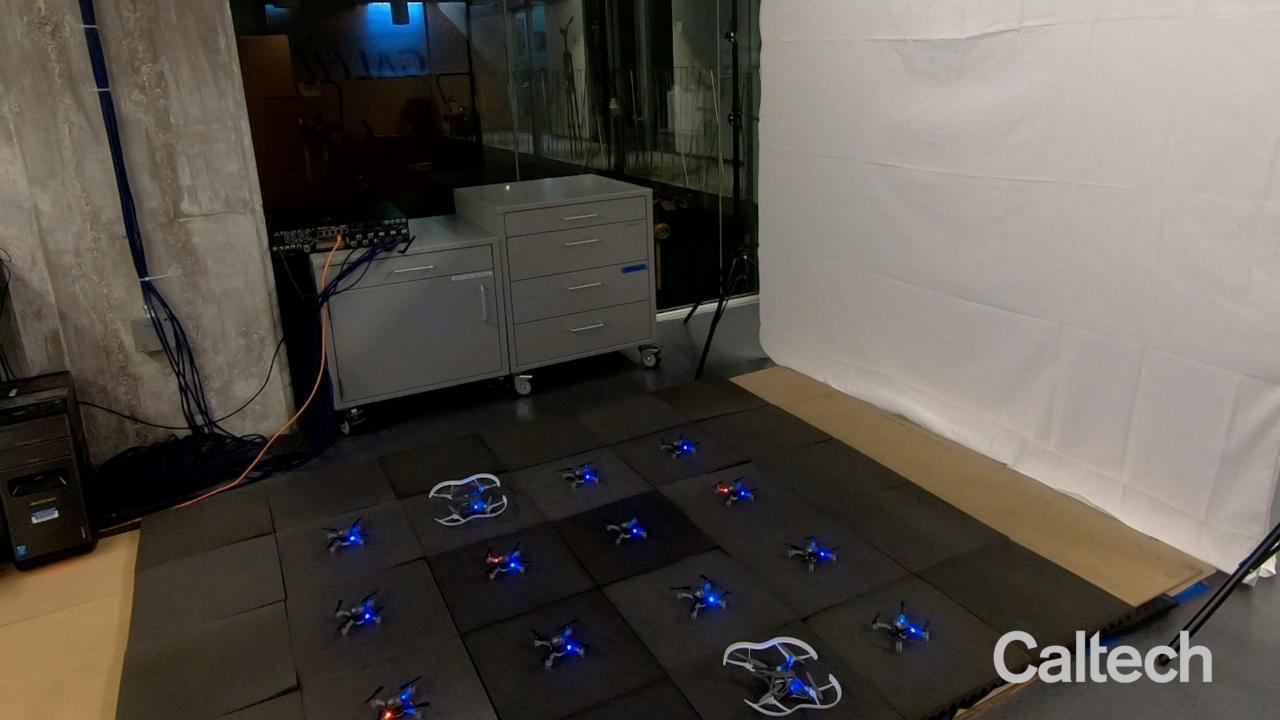
Controller Design (simplified)

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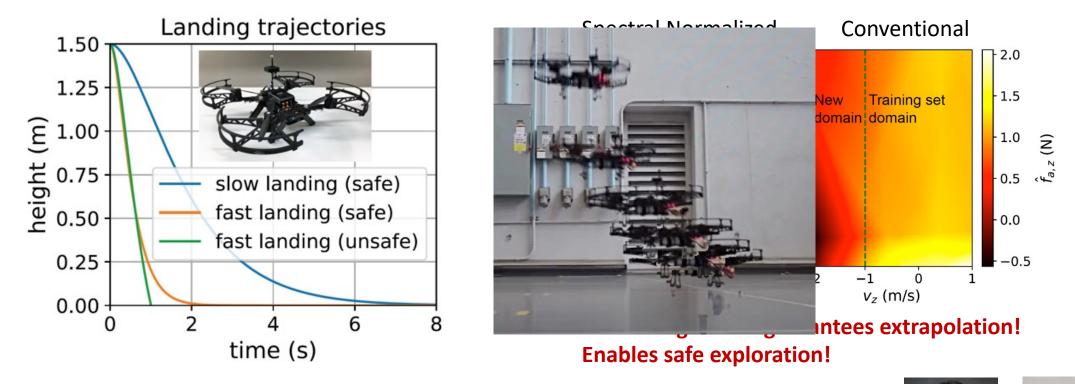








Aside: Robust Regression for Safe Exploration







Angie Liu

Yashwanth Nakka

Robust Regression for Safe Exploration in Control,

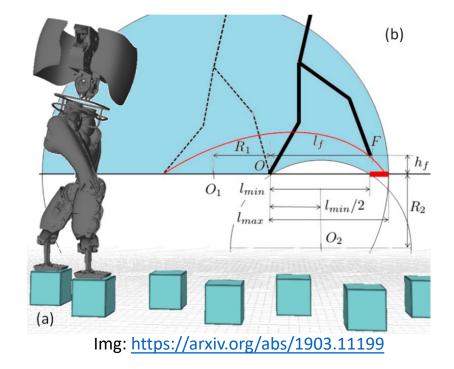
Angie Liu, Guanya Shi, Soon-Jo Chung, Anima Anandkumar, Yisong Yue

Chance-Constrained Trajectory Optimization for Safe Exploration and _______ Ionlinear Systems,

Yashwanth Kumar Nakka, Angie Liu, Guanya Shi, Anima Anandkumar, Yisong Yue, Soon-Jo Chung, R-AL 2021

Aside: Learning Control Lyapunov/Barrier Functions

- CLFs & CBFs encode low-dim projection of dynamics
- Learn CLF/CBFs?
- Stability/safety under uncertainty?



Episodic Learning with Control Lyapunov Functions for Uncertain Robotic Systems
Andrew J. Taylor, Victor D. Dorobantu, Hoang M. Le, Yisong Yue, Aaron D. Ames. IROS 2019.
A Control Lyapunov Perspective on Episodic Learning via Projection to State Stability
Andrew J. Taylor, Victor D. Dorobantu, Meera Krishnamoorthy, Hoang M. Le, Yisong Yue, Aaron D. Ames. CDC 2019.
Learning for Safety-Critical Control with Control Barrier Functions
Andrew Taylor, Andrew Singletary, Yisong Yue, Aaron Ames. L4DC 2020.
A Control Barrier Perspective on Episodic Learning via Projection-to-State Safety
Andrew J. Taylor, Andrew Singletary, Yisong Yue, Aaron D. Ames. L-CSS 2020.



Andrew

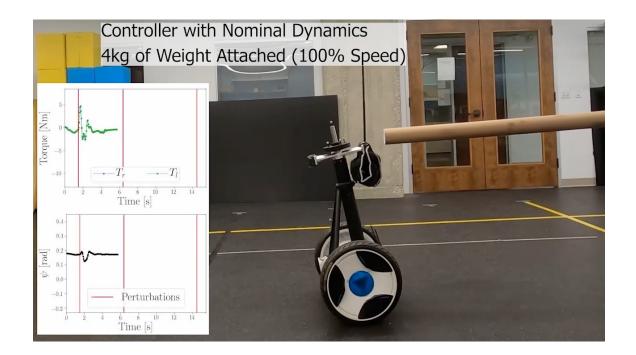
Taylor



Victor

Dorobantu





Dynamic Environments

[Neural-Fly, Science Robotics 2022]

Meta-learning + Adaptive Control





Sharp Non-Linearities

https://arxiv.org/abs/2103.04548 [IROS 2021]

Learn Continuous-time Models



Ugo Rosolia

Summary: Dynamics Learning

- Learn residual dynamics
- Control Lipschitz constant
- Standard controller design
- Extend to complex settings
- Robust regression for safe exploration

(data efficient)

(imposes compatible structure)

(inherits guarantees)

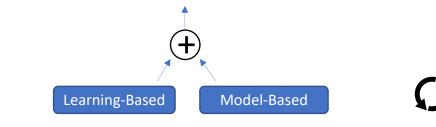
(multi-agent, meta-learning, continuous-time, etc.)

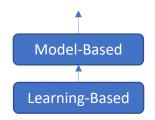
(provable limited extrapolation)

Integration of Learning at Varying Levels

Integration in control/action

Integration in dynamics modeling







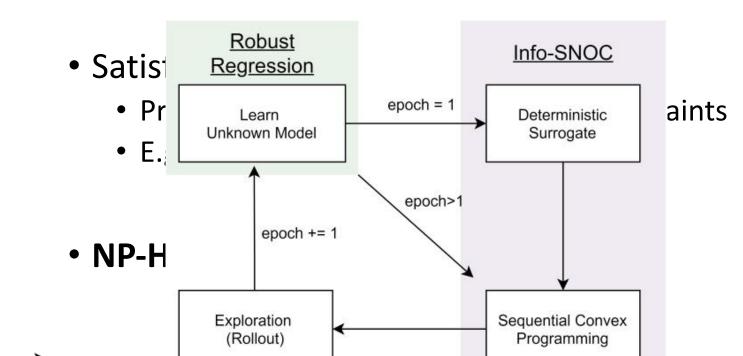
Model-Based Planning

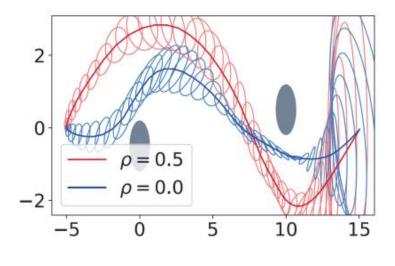
• Environment model is given

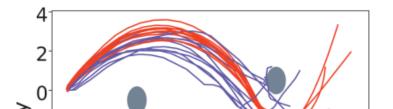
1

 $s_{t+1} = F(s_t, u_t) + \epsilon$

• Design global plan (aka trajectory)







Optimization as Sequential Decision Making

- Many Solvers are Sequential
 - Tree-Search
 - Greedy
 - Gradient Descent
- Can view solver as "agent" or "policy"
 - State = intermediate solution
 - Find a state with high reward (solution)
 - Learn better local decision making

Optimization as Sequential Decision Making

Learning Search Policy

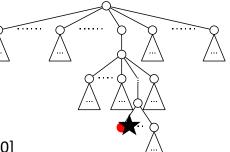
- Learning to Search via Retrospective Imitation [arXiv]
- Co-training for Policy Learning [UAI 2019]
- GLAS: Global-to-Local Safe Autonomy Synthesis [RA-L 2020]
- A General Large Neighborhood Search Framework for Solving Integer Programs [NeurIPS 2020]

Learning Value Function

- MLNav: Learning to Safely Navigate on Martian Terrains [R-AL 2022]
- Learning to Make Decisions via Submodular Regularization [ICLR 2021]

Learning to Infer

- Iterative Amortized Inference [ICML 2018]
- A General Method for Amortizing Variational Filtering [NeurIPS 2018]
- Iterative Amortized Policy Optimization [NeurIPS 2021]







Jialin Song Ben Riviere

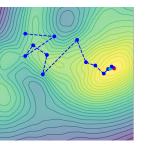






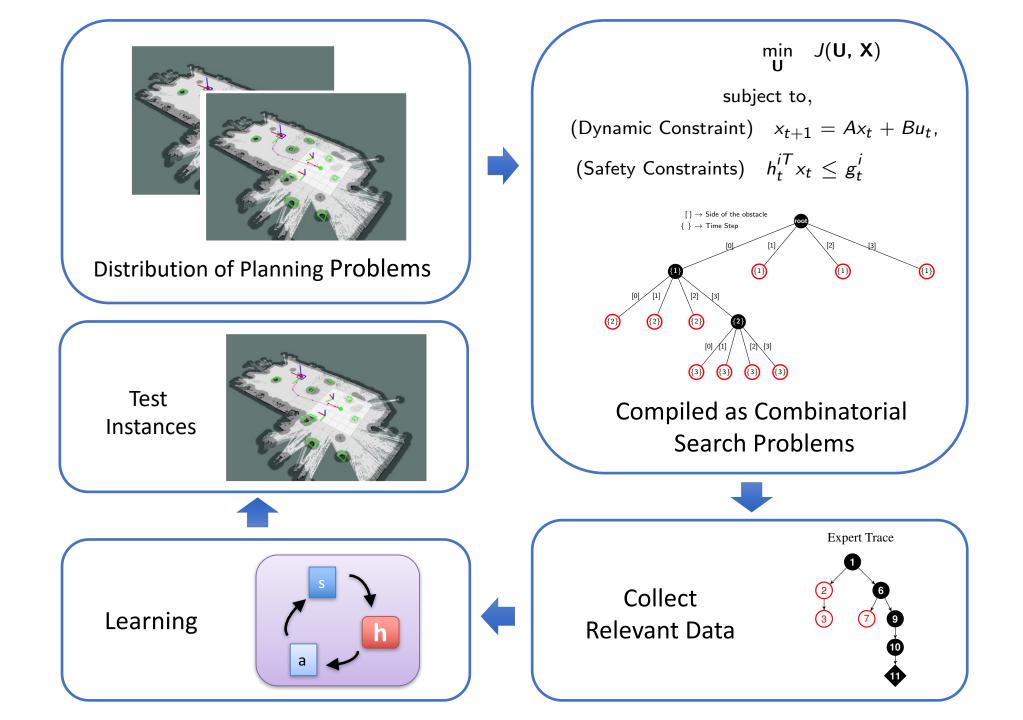
Ayya Alieva

_{/a} Shreyansh Daftry

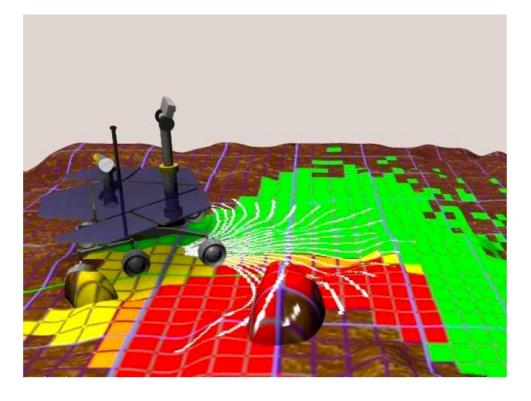


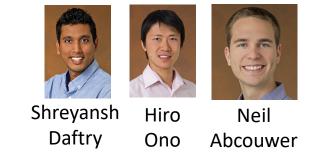


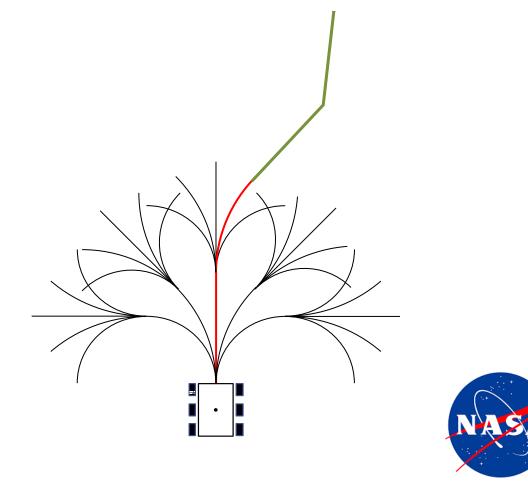
Joe Marino



MLNav: Learning-Augmented Rover Navigation







MLNav: Learning to Navigate on Martian Terrains, Shreyansh Daftry et al., R-AL 2022



Learned Decentralized Planner (enforcing safety)

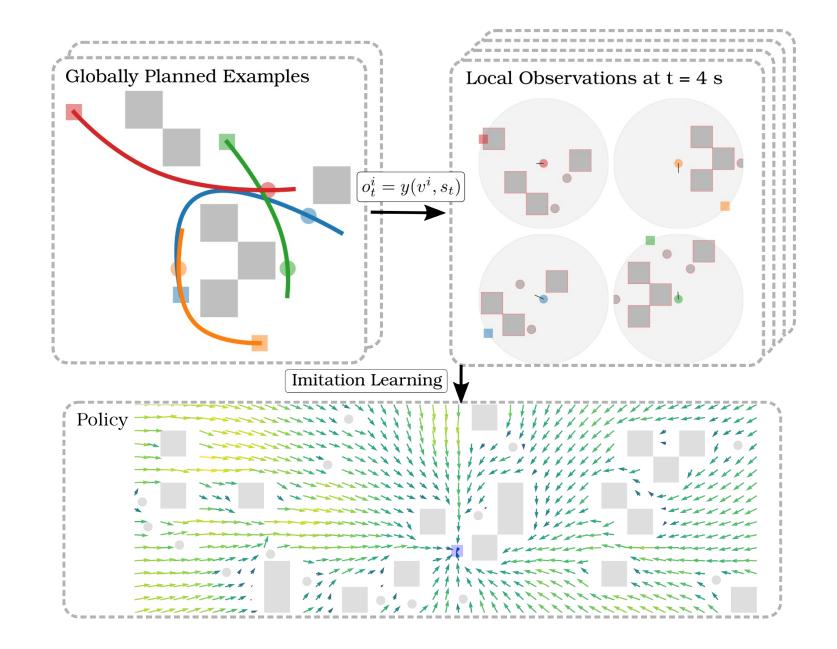




Ben Riviere



GLAS: Global-to-Local Safe Autonomy Synthesis for Multi-Robot Motion Planning with End-to-End Learning, Benjamin Rivière, et al., R-AL 2020



5. Deploy: Six robots navigating an obstacle course.

2x

Learned ODE-based Policy

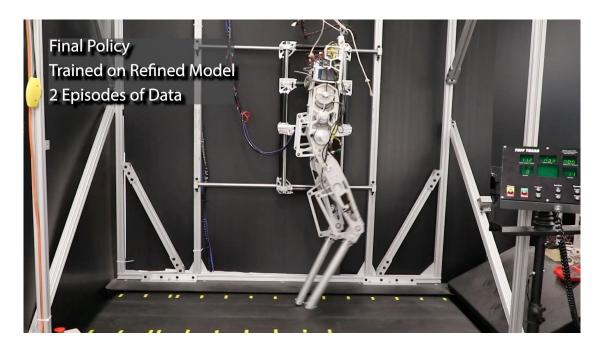
Neural Gaits: Learning Bipedal Locomotion via Control Barrier Functions and Zero Dynamics Policoes Jimenez Rodriguez, Csomay-Shanklin, et al., L4DC 2022

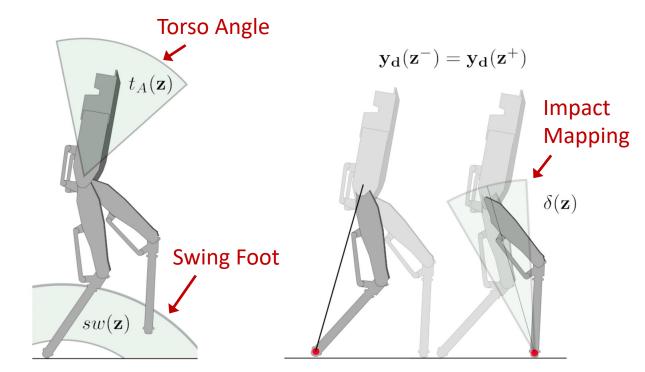


lvan Jimenez Rodriguez



Noel Csomay-Shanklin



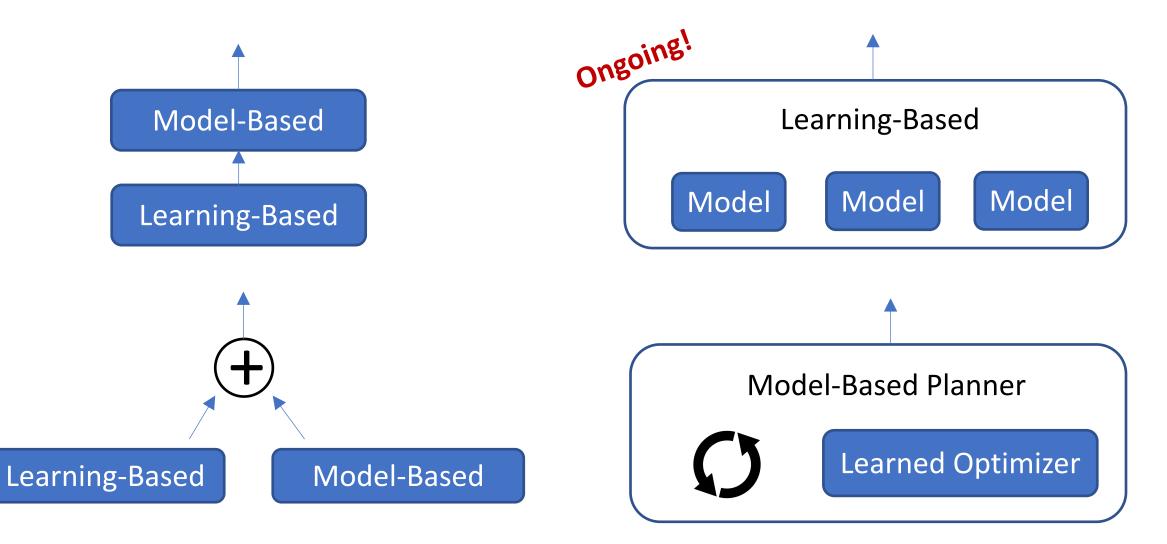


Continuous

Discrete

- **Barriers** induce control-theoretic safety conditions
- Conventional: complicated ODE-based optimization
- Learn policy as **Neural ODE**
 - Fast run-time gait generation
 - Satisfies safety guarantees

Blending Models/Rules & Black-Box Learning



Collaborators



Song

Ravi

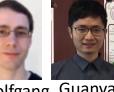
Lanka



Le



Taylor



Wolfgang Guanya Shi Dorobantu Hoenig Cheng

Richard Abhinav



Liu

Yashwanth Ben

Riviere







Michael lvan O'Connell Jimenez Rodriguez





Voloshin Csomay

-Shanklin

Anima



Noel Jimmy

Chen

Marino

Andrew Milan Kang Cvitkovic



Siddarth Aadyot Venkatraman Bhatnagar

Zhao

Ono

Albert Meera

Verma

Krishnamoorthy Rosolia

Ugo Tyler del Sesto







Xichen Alex Shi

Aiden Aceves



Stephen

Mavo



Anandkumar Chung







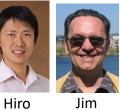
Orosz

Lucas

Igel



Kamyar Stephan Mandt Azizzadenesheli Chaudhuri



Little



Abcouwer



Carr

Yu

Alessandro

lalongo

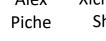
Nakka



Daftry

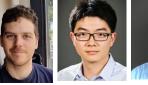


Bistra Yuxin Dilkina Chen











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Thanks!







